





CLASS : XIth DATE :

Solutions

SUBJECT : MATHS DPP NO. :1

Topic :-probability

1 (a) Since the given distribution is a probability distribution $\therefore 0 + 2p + 2p + 3p + p^2 + 2p^2 + 7p^2 + 2p = 1$ $\Rightarrow 10 p^{2} + 9 p - 1 = 0 \Rightarrow (10 p - 1)(p + 1) = 0 \Rightarrow p = 1/10$ 2 (a) We have, $P(E \cap F) = \frac{1}{12}$ and $P(\overline{E} \cap \overline{F}) = \frac{1}{2}$ $\Rightarrow P(E)P(F) = \frac{1}{12} \text{ and } P(\overline{E})P(\overline{F}) = \frac{1}{2}$ [\because *E* and *F* are independent events] $\Rightarrow P(E)P(F) = \frac{1}{12} \text{ and } \{1 - P(E)\}\{1 - P(F)\} = \frac{1}{2}$ $\Rightarrow P(E)P(F) = \frac{1}{12} \text{ and } 1 - \{P(E) + P(F)\} + P(E)P(F) = \frac{1}{2}$ $\Rightarrow P(E)P(F) = \frac{1}{12} \text{ and } 1 - \{P(E) + P(F)\} + \frac{1}{12} = \frac{1}{2}$ $\Rightarrow P(E)P(F) = \frac{1}{12} \text{ and } P(E) + P(F) = \frac{7}{12}$ The quadratic equation having P(E) and P(F) as its roots is $x^{2} - \{P(E) + P(F)\}x + P(E)P(F) = 0$ $\Rightarrow x^{2} - \frac{7}{12}x + \frac{1}{12} = 0 \Rightarrow x = \frac{1}{3}, \frac{1}{4}$: $P(E) = \frac{1}{3}$ and $P(F) = \frac{1}{4}$ or, $P(E) = \frac{1}{4}$ and $P(F) = \frac{1}{3}$ 3 (a) We have, $p = Probability of getting at least 3 in a throw = \frac{4}{6} = \frac{2}{3}$ $\therefore q = 1 - p = \frac{1}{2}$ Required probability $= {}^{6}C_{3}\left(\frac{2}{3}\right)^{3}\left(\frac{1}{3}\right)^{3} + {}^{6}C_{4}\left(\frac{2}{3}\right)^{4}\left(\frac{1}{3}\right)^{2} + {}^{6}C_{5}\left(\frac{2}{3}\right)^{5}\left(\frac{1}{3}\right) + {}^{6}C_{6}\left(\frac{2}{3}\right)^{6}$ $= 41 \times \frac{-}{3^6}$ 4 (c) Given $P(A \cup B) = 0.6, P(A \cap B) = 0.3$ $\therefore P(A') + P(B')$ $= 1 - P(A) + 1 - P(B) = 2 - \{P(A) + P(B)\}$ $= 2 - \{P(A \cup B) + P(A \cap B)\}$ $= 2 - \{0.6 + 0.3\} = 2 - 0.9 = 1.1$ 6 (c)





Given, $P(A) = \frac{1}{3}$, $P(B) = \frac{1}{3}$ and $P(C) = \frac{1}{4}$: $P(A') = \frac{2}{3}, P(B') = \frac{2}{3} \text{ and } P(C') = \frac{3}{4}$ Now, $P(A' \cap B' \cap C') = P(A')P(B')P(C')$ [:: A, B and C are independent events] $=\frac{2}{3}\times\frac{2}{3}\times\frac{3}{4}=\frac{1}{3}$ 7 (c) Total number of elementary events = $6^3 = 216$ Favourable number of elementary events = Coeff. of x^{15} in $(x^1 + x^2 + x^3 + \dots + x^6)^3$ = Coeff. of x^{15} in $x^3 \left(\frac{1-x^6}{1-x}\right)^3$ = Coeff. of x^{12} in $(1 - 3x^6 + 3x^{12} - x^{18})(1 - x)^{-3}$ = Coeff. of x^{12} in $(1 - x)^{-3} - 3$ Coeff. of x^{6} in $(-x)^{-3}$ + 3 Coeff. of x^0 in $(1 - x)^{-3}$ $= {}^{12+3-1}C_{3-1} - 3 \times {}^{6+3-1}C_{3-1} + 3 = {}^{14}C_2 - 3$ $= {}^{14}C_2 - 3 \times {}^{8}C_2 + 3 = 91 - 84 + 3 = 10$ So, required probability $=\frac{10}{216}=\frac{5}{108}$ 8 (d) For a Poisson distribution, mean = variance \Rightarrow Variance = 16 \therefore Standard deviation= $\sqrt{Variance}$ $=\sqrt{16} = 4$ 9 (a) The sum of two numbered on a dice is odd only, whence once is odd and second is even. ∴ Required probability $= 2 \times \text{probability of odd number}$ ×probability of even number [:Here, we multiply by 2 because either the even number is on first or second dice.] $= 2 \times \left(\frac{5}{6}\right) \times \left(\frac{1}{6}\right) = \frac{5}{18}$ 10 (b) In binomial distribution, variance = npq and mean = np. From the given condition npq = 3 and np = 4 $\therefore \frac{npq}{np} = \frac{3}{4}$ $\Rightarrow q = \frac{3}{4}, p = \frac{1}{4} \text{ and } n = 16$ Probability of exactly six success = ${}^{16}C_6 \left(\frac{1}{a}\right)^6 \left(\frac{3}{a}\right)^{10}$ 11 (a) Since A and B are independent events $\therefore P(A \cap B) = \frac{1}{6} \text{ and } P(\overline{A} \cap \overline{B}) = \frac{1}{3}$ $\Rightarrow P(A)P(B) = \frac{1}{6} \text{ and } P(\overline{A})P(\overline{B}) = \frac{1}{3}$ $\Rightarrow P(A)P(B) = \frac{1}{6} \text{ and } \{(1 - P(A))\}\{(1 - P(B))\} = \frac{1}{3}$ $\Rightarrow 1 - [P(A) + P(B)] + \frac{1}{6} = \frac{1}{3}$



 $\Rightarrow P(A) + P(B) = \frac{5}{6}$ Solving $P(A) P(B) = \frac{1}{6}$ and $P(A) + P(B) = \frac{5}{6}$, we get $P(A) = \frac{1}{2}$ and $P(B) = \frac{1}{3}$ or, $P(A) = \frac{1}{3}$ and $P(B) = \frac{1}{2}$ Hence, option (a) is correct 12 (b) Since, A and B are independent events $\therefore P(A)P(B) = \frac{1}{6} \text{ and } P(\overline{A})P(\overline{B}) = \frac{1}{3}$ $\Rightarrow [1 - P(A)][1 - P(B)] = \frac{1}{3}$ $\Rightarrow 1 - [P(A) + P(B)] + P(A)P(B) = \frac{1}{3}$ $\Rightarrow 1 + \frac{1}{6} - \frac{1}{3} = P(A) + P(B)$ $\Rightarrow P(A) + P(B) = \frac{5}{6}$ $\Rightarrow P(A) = \frac{1}{2}, P(B) = \frac{1}{3},$ or $P(A) = \frac{1}{3}$, $P(B) = \frac{1}{2}$ 13 (a) $7^1 = 7, 7^2 = 49, 7^3 = 343, 7^4 = 2401,$ Therefore, for $7^r, r \in N$ the no. ends at unit place 7, 9, 3, 1, 7,.... \therefore 7^{*m*} + 7^{*n*} will be divisible by 5, if it end at 5 or 0. But it cannot end at 5. Also it cannot end at 0. For this *m* and *n* should be as follows : mп 4r + 21 4r2 4r + 14r + 33 4r + 24r4r + 34r + 1For any given value of *m*, there will be 25 values of *n*. Hence, the probability of the required event is $\frac{100 \times 25}{100 \times 100} = \frac{1}{4}$. 14 (c) A dice is thrown thrice, $n(S) = 6 \times 6 \times 6$ Favorable events of $\omega^{r_1} + \omega^{r_2} + \omega^{r_3} = 0$ *ie*, (r_1, r_2, r_3) are ordered triplets which can take values, (1, 2, 3), (1, 5, 3), (4, 2, 3), (4, 5, 3))(1, 2, 6), (1, 5, 6), (4, 2, 6), (4, 5, 6)*ie*, 8 ordered triplets and each can be arranged in 3! ways = 6 $\therefore n(E) = 8 \times 6$ $\Rightarrow P(E) = \frac{8 \times 6}{6 \times 6 \times 6}$ 2 $= \frac{1}{9}$ 15 (c) We have, Total number of functions from *A* to itself = n^n Out of these functions, *n*! Function are injections

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So, required probability $= \frac{n!}{n^n} = \frac{(n-1)!}{n^{n-1}}$ 16 (d)

Let A_i (i = 1,2,3,4) be the event that the urn contains 2,3,4 or 5 white balls and E the event that two white balls are drawn. Since the four events A_1, A_2, A_3, A_4 are equally likely. Therefore, $P(A_i) = \frac{1}{4}$, i = 1,2,3,4 We have,

 $P(E/A_1) =$ Prob. that the urn contains 2 white balls and both have been drawn

 $\Rightarrow P(E/A_1) = \frac{{}^2C_2}{{}^5C_2} = \frac{1}{10}$ Similarly, we have

$$P(E/A_2) = \frac{{}^{3}C_2}{{}^{5}C_2} = \frac{3}{10}, P(E/A_3) = \frac{{}^{4}C_2}{{}^{5}C_2} = \frac{3}{5}, P(E/A_4) = \frac{{}^{5}C_2}{{}^{5}C_2} = 1$$
Required probability = $P(A_1/E) = -\frac{P(A_4)P(E/A_4)}{{}^{5}C_2} = 1$

Required probability =
$$P(A_4/E) = \frac{1}{\sum_{i=1}^{4} P(A_i)P(E/A_i)}$$

 $=\frac{\frac{1}{4}\times 1}{\frac{1}{4}\left(\frac{1}{10}+\frac{3}{10}+\frac{3}{5}+1\right)}=\frac{1}{2}$

17 **(b)**

There are 11 letters in word 'PROBABILITY' out of which 1 can be selected in ${}^{11}C_1$ ways.

There are four vowels viz. *A*, *I*, *O*. Therefore,

Number of ways of selecting a vowel = ${}^{4}C_{1} = 4$ Hence, required probability = $\frac{4}{11}$

18 **(b)**

If the show a six, then number of outcomes =8 If die not show a six. Then number of outcomes=2 \therefore Sample space = 1 × 8 + 2 × 5 = 18 points 19 (c) Given, n = 6 and P(X = 2) = 9P(X = 4) $\Rightarrow {}^{6}C_{2}p^{2}q^{4} = 9.{}^{6}C_{4}p^{4}q^{2}$ $\Rightarrow 9p^{2} = q^{2}$ $\Rightarrow P = \frac{1}{3}q$ \therefore We know that p + q = 1

$$\Rightarrow \frac{q}{3} + q = 1$$

$$\Rightarrow q = \frac{3}{4} \text{ and } p = \frac{1}{4}$$

$$\therefore \text{ Variance} = npq$$

$$= 6.\frac{1}{4}.\frac{3}{4} = \frac{9}{8}$$

20 (a)

Required probibility = $\frac{{}^{5}C_{1} \times {}^{8}C_{1}}{{}^{13}C_{2}} + \frac{{}^{5}C_{2}}{{}^{13}C_{2}} = \frac{25}{39}$

ACHING



ANSWER-KEY										
Q.	1	2	3	4	5	6	7	8	9	10
A.	А	А	А	С	А	С	С	D	А	В
Q.	11	12	13	14	15	16	17	18	19	20
A.	А	В	А	С	С	D	В	В	С	А

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