



DPP

DAILY PRACTICE PROBLEMS

CLASS : XIIth

DATE :

SOLUTION

SUBJECT : MATHS

DPP NO. :2

Topic :-MATRICES

1 (a)

$$A^2 = 2A - I$$

$$\therefore A^2 A = 2AA - IA$$

$$= 2A^2 - A = 2(2A - I) - A$$

$$\Rightarrow A^3 = 3A - 2I$$

$$\Rightarrow A^3 \cdot A = 3AA - 2IA = 3(2A - I) - 2A$$

$$\Rightarrow A^4 = 4A - 3I$$

$$\text{Similarly, } A^n = nA - (n - 1)I$$

2 (d)

$$\det(M_r) = \begin{vmatrix} r & r-1 \\ r-1 & r \end{vmatrix} = 2r - 1$$

$$\sum_{r=1}^{2007} \det(M_r) = 2 \sum_{r=1}^{2007} r - 2007$$

$$= 2 \times \frac{2007 \times 2008}{2} - 2007 = (2007)^2$$

3 (a)

$$\text{Let } A = \begin{bmatrix} 0 & 1 & -1 \\ -1 & 0 & 2 \\ 1 & -2 & 0 \end{bmatrix}$$

$$\therefore |A| = \begin{vmatrix} 0 & 1 & -1 \\ -1 & 0 & 2 \\ 1 & -2 & 0 \end{vmatrix}$$

$$= 0 \begin{vmatrix} 0 & 2 \\ -2 & 0 \end{vmatrix} - 1 \begin{vmatrix} -1 & 2 \\ 1 & 0 \end{vmatrix} + 2 \begin{vmatrix} -1 & 0 \\ 1 & -2 \end{vmatrix}$$

$$= 0 + 2 - 2 = 0$$

$$\Rightarrow |A| = 0$$

$$\text{Now, } (\text{adj } A)B = \begin{bmatrix} 4 & 2 & 2 \\ 2 & 1 & 1 \\ 2 & 1 & -1 \end{bmatrix} \begin{bmatrix} 1 \\ -2 \\ 3 \end{bmatrix}$$

$$= \begin{bmatrix} 4 - 4 + 6 \\ 2 - 2 + 3 \\ 2 - 2 - 3 \end{bmatrix} = \begin{bmatrix} 6 \\ 3 \\ -3 \end{bmatrix} \neq 0$$

\therefore This system of equation is inconsistent, so it has no solution

5 (c)

$$\text{Given, } D = \text{diag}(d_1, d_2, d_3, \dots, d_n)$$

$$\Rightarrow D^{-1} = \text{diag}(d_1^{-1}, d_2^{-1}, \dots, d_n^{-1})$$

6 (a)

We have,

$$a = \begin{bmatrix} 1 & a \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow A^n = \begin{bmatrix} 1 & na \\ 0 & 1 \end{bmatrix} \quad [\text{Using PMI}]$$



$$\Rightarrow \frac{1}{n} A^n = \begin{bmatrix} \frac{1}{n} & a \\ 0 & \frac{1}{n} \end{bmatrix} \Rightarrow \lim_{n \rightarrow \infty} \frac{1}{n} A^n = \begin{bmatrix} 0 & a \\ 0 & 0 \end{bmatrix}$$

7 (d)

The given system of equations are

$$2x + y - 5 = 0 \quad \dots(i)$$

$$x - 2y + 1 = 0 \quad \dots(ii)$$

$$\text{and } 2x - 14y - a = 0 \quad \dots(iii)$$

This system is consistent.

$$\therefore \begin{vmatrix} 2 & 1 & -5 \\ 1 & -2 & 1 \\ 2 & -14 & -a \end{vmatrix} = 0$$

$$\Rightarrow 2(2a + 14) - 1(-a - 2) - 5(-14 + 4) = 0$$

$$\Rightarrow 4a + 28 + a + 2 + 50 = 0$$

$$\Rightarrow 5a = -80 \quad \Rightarrow \quad a = -16$$

8 (d)

The system of given equations has no solution, if $\begin{vmatrix} \alpha & 1 & 1 \\ 1 & \alpha & 1 \\ 1 & 1 & \alpha \end{vmatrix} = 0$

Applying $C_1 \rightarrow C_1 + C_2 + C_3$ and taking common $(\alpha + 2)$ from C_1 , we get

$$(\alpha + 2) \begin{vmatrix} 1 & 1 & 1 \\ 1 & \alpha & 1 \\ 1 & 1 & \alpha \end{vmatrix} = 0$$

Applying $R_2 \rightarrow R_2 - R_1, R_3 \rightarrow R_3 - R_1$

$$\Rightarrow (\alpha + 2) \begin{vmatrix} 1 & 1 & 1 \\ 0 & \alpha - 1 & 0 \\ 0 & 0 & \alpha - 1 \end{vmatrix} = 0$$

$$\Rightarrow (\alpha + 2)(\alpha - 1)^2 = 0$$

$$\Rightarrow \alpha = 1, -2$$

But $\alpha = 1$ makes given three equations same. So, the system of equation have infinite solution. So, answer is $\alpha = -2$ for which the system of equations has no solution

10 (b)

$$\text{Given, } A = \begin{bmatrix} x & 1 \\ 1 & 0 \end{bmatrix}$$

$$\therefore A^2 = \begin{bmatrix} x & 1 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x & 1 \\ 1 & 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x^2 + 1 & x \\ x & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\Rightarrow x^2 + 1 = 1, x = 0$$

$$\Rightarrow x = 0$$

11 (a)

Given that, $A^{-1} = \lambda (\text{adj } A)$

On comparing with $A^{-1} = \frac{1}{|A|} A$ we get

$$\lambda = \frac{1}{|A|}$$

$$\text{Now, } |A| = \begin{vmatrix} 0 & 3 \\ 2 & 0 \end{vmatrix} = 0 - 6 = -6$$

$$\Rightarrow \lambda = -\frac{1}{6}$$

12 (d)

$$a_{11}C_{11} + a_{12}C_{12} + a_{13}C_{13} + a_{14}C_{14} = |A|$$

13 (d)

Given equation are $x + y + z = 6, x + 2y + 3z = 10$ and $x + 2y + \lambda z = 10$



Since, it is consistent.

$$\therefore \begin{vmatrix} 1 & 1 & 1 \\ 1 & 2 & 3 \\ 1 & 2 & \lambda \end{vmatrix} = 0$$

$$\Rightarrow 1(2\lambda - 6) - 1(\lambda - 3) + 1(2 - 2) = 0$$

$$\Rightarrow \lambda - 3 = 0 \Rightarrow \lambda = 3$$

14 (b)

$$A^2 = \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = 2 \begin{bmatrix} 1 & 1 \\ 1 & 1 \end{bmatrix} = 2A$$

$$\therefore A^4 = 2A \cdot 2A = 4A^2 = 4 \times 2A = 2^3 A$$

Similarly, $A^8 = 2^7 A$

$$\Rightarrow A^{100} = 2^{99} A$$

15 (d)

$$\text{Let } A = \begin{bmatrix} \cos 2\theta & -\sin 2\theta \\ \sin 2\theta & \cos 2\theta \end{bmatrix}$$

$$\therefore |A| = \cos^2 2\theta + \sin^2 2\theta = 1$$

$$\text{and adj } A = \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{1} \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$$

$$= \begin{bmatrix} \cos 2\theta & \sin 2\theta \\ -\sin 2\theta & \cos 2\theta \end{bmatrix}$$

18 (a)

Given equation can be written as,

$$2X = \begin{bmatrix} 3 & 8 \\ 7 & 2 \end{bmatrix} - \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$$

$$\Rightarrow 2X = \begin{bmatrix} 2 & 6 \\ 4 & -2 \end{bmatrix} = 2 \begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix}$$

$$\Rightarrow X = \begin{bmatrix} 1 & 3 \\ 2 & -1 \end{bmatrix}$$

19 (c)

We have,

$$AB = 0$$

$$\Rightarrow |AB| = 0$$

$$\Rightarrow |A| |B| = 0$$

$$\Rightarrow |A| = 0 \text{ or } |B| = 0$$

Let $A = \begin{bmatrix} 1 & 0 \\ 0 & 0 \end{bmatrix}$, $B = \begin{bmatrix} 0 & 0 \\ 0 & 1 \end{bmatrix}$. Then, $AB = 0$. But $A \neq 0$, $B \neq 0$

20 (b)

$$\text{Given, } A = \begin{bmatrix} 1 & -1 & -2 \\ 2 & 1 & 1 \\ 4 & -1 & -2 \end{bmatrix}$$

$$\therefore A^{-1} = \frac{1}{3} \begin{bmatrix} -1 & 0 & 1 \\ 8 & 6 & -5 \\ -6 & -3 & 3 \end{bmatrix}$$

$$\text{Now, } A^{-1}D = \frac{1}{3} \begin{bmatrix} -1 & 0 & 1 \\ 8 & 6 & -5 \\ -6 & -3 & 3 \end{bmatrix} \begin{bmatrix} 3 \\ 5 \\ 11 \end{bmatrix} = \frac{1}{3} \begin{bmatrix} 8 \\ -1 \\ 0 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 8/3 \\ -1/3 \\ 0 \end{bmatrix}$$

ANSWER-KEY

Q.	1	2	3	4	5	6	7	8	9	10
A.	A	D	A	A	C	A	D	D	B	B
Q.	11	12	13	14	15	16	17	18	19	20
A.	A	D	D	B	D	C	A	A	C	B

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