

## DPP

DAILY PRACTICE PROBLEMS

**CLASS : XIIth**  
**DATE :**

**SUBJECT : MATHS**  
**DPP NO. : 3**

### Topic :-DIFFERENTIAL EQUATIONS

- Solution of the differential equation  $\frac{dy}{dx} + y \sec^2 x = \tan x \sec^2 x$  is
  - $y = \tan x - 1 + ce^{-\tan x}$
  - $y^2 = \tan x - 1 + ce^{\tan x}$
  - $ye^{\tan x} = \tan x - 1 + c$
  - $ye^{-\tan x} = \tan x - 1 + c$
- The differential equation  $y \frac{dy}{dx} + x = a$  ( $a$  is any constant) represents
  - A set of circles having centre on the  $y$  -axis
  - A set of circles on the  $x$  -axis
  - A set of ellipses
  - None of these
- The equation of the curve for which the square of the ordinate is twice the rectangle contained by the abscissa and the intercept of the normal on  $x$ -axis and passing through  $(2, 1)$  is
  - $x^2 + y^2 - x = 0$
  - $4x^2 + 2y^2 - 9y = 0$
  - $2x^2 + 4y^2 - 9x = 0$
  - $4x^2 + 2y^2 - 9x = 0$
- The general solution of  $ydx - xdy - 3x^2y^2e^{x^3} dx = 0$ , is equal to
  - $\frac{x}{y} = e^{x^3} + C$
  - $\frac{y}{x} = e^{x^3} + C$
  - $xy = e^{x^3} + C$
  - $xy = e^x + C$
- The solution of  $\frac{dy}{dx} = \frac{ax+h}{by+k}$  represents a parabola, when
  - $a = 0, b = 0$
  - $a = 1, b = 2$
  - $a = 0, b \neq 0$
  - $a = 2, b = 1$
- The differential equation of all ellipses centred at the origin is
  - $y_2 + x y_1^2 - y y_1 = 0$
  - $xy y_2 + x y_1^2 - y y_1 = 0$
  - $y y_2 + x y_1^2 - x y_1 = 0$
  - None of these
- If  $y = ax^{n+1}$ , then  $x^2 \frac{d^2y}{dx^2}$  is equal to
  - $n(n-1)$
  - $n(n+1)y$
  - $ny$
  - $n^2y$
- The differential equation of the family of curves  $y = a \cos(x + b)$  is
  - $\frac{d^2y}{dx^2} - y = 0$
  - $\frac{d^2y}{dx^2} + y = 0$
  - $\frac{d^2y}{dx^2} + 2y = 0$
  - None of these
- If  $y(t)$  is a solution of  $(1+t) \frac{dy}{dt} - ty = 1$  and  $y(0) = -1$ , then  $y(1)$  is equal to
  - $-\frac{1}{2}$
  - $e + \left(\frac{1}{2}\right)$
  - $e - \frac{1}{2}$
  - $\frac{1}{2}$

10. The integrating factor of the differential equation  $\frac{dy}{dx} + \frac{y}{(1-x)\sqrt{x}} = 1 - \sqrt{x}$  is  
 a)  $\frac{1-\sqrt{x}}{1+\sqrt{x}}$       b)  $\frac{1+\sqrt{x}}{1-\sqrt{x}}$       c)  $\frac{1-x}{1+x}$       d)  $\frac{\sqrt{x}}{1-\sqrt{x}}$
11. The solution of the differential equation  $(x^2 + y^2)dx = 2xy dy$  is (here  $c$  is an arbitrary constant)  
 a)  $x^2 + y^2 = cy$       b)  $c(x^2 - y^2) = x$       c)  $x^2 - y^2 = cy$       d)  $x^2 + y^2 = cx$
12. The real value of  $n$  for which the substitution  $y = u^n$  will transform the differential equation  $2x^4y \frac{dy}{dx} + y^4 = 4x^6$  into a homogenous equation is  
 a)  $1/2$       b)  $1$       c)  $3/2$       d)  $2$
13. The differential equation satisfied by the family of curves  $y = ax \cos\left(\frac{1}{x} + b\right)$  where  $a, b$  are parameters is  
 a)  $x^2y_2 + y = 0$       b)  $x^4y_2 + y = 0$       c)  $xy_2 - y = 0$       d)  $x^4y_2 - y = 0$
14. The solution of the differential equation  $\frac{dy}{dx} = x \log x$  is  
 a)  $y = x^2 \log x - \frac{x^2}{2} + c$       b)  $y = \frac{x^2}{2} \log x - \frac{x^2}{4} + c$   
 c)  $y = \frac{x^2}{2} + \frac{x^2}{2} \log x + c$       d) None of these
15. Differential equation of  $y = \sec(\tan^{-1} x)$  is  
 a)  $(1 + x^2) \frac{dy}{dx} = y + x$       b)  $(1 + x^2) \frac{dy}{dx} = y - x$       c)  $(1 + x^2) \frac{dy}{dx} = xy$       d)  $(1 + x^2) \frac{dy}{dx} = \frac{x}{y}$
16. Solution of the differential equation  $\frac{dy}{dx} \tan y = \sin(x + y) + \sin(x - y)$  is  
 a)  $\sec y + 2 \cos x = c$       b)  $\sec y - 2 \cos x = c$       c)  $\cos y - 2 \sin x = c$       d)  $\tan y - 2 \sec x = c$
17. The differential equation of the family of parabolas with focus at the origin and the  $x$ -axis as axis, is  
 a)  $y \left(\frac{dy}{dx}\right)^2 + 4x \frac{dy}{dx} = 4y$       b)  $-y \left(\frac{dy}{dx}\right)^2 = 2x \frac{dy}{dx} - y$   
 c)  $y \left(\frac{dy}{dx}\right)^2 + y = 2xy \frac{dy}{dx}$       d)  $y \left(\frac{dy}{dx}\right)^2 + 2xy \frac{dy}{dx} + y = 0$
18. The integrating factor of the differential equation  $\frac{dy}{dx} + y = \frac{1+y}{x}$ , is  
 a)  $\frac{x}{e^x}$       b)  $\frac{e^x}{x}$       c)  $x e^x$       d)  $e^x$
19. The differential equation of all coaxial parabola  $y^2 = 4a(x - b)$ , where  $a$  and  $b$  are arbitrary constants, is  
 a)  $y \frac{d^2y}{dx^2} + \frac{dy}{dx} = 1$       b)  $y \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 1$       c)  $y \frac{d^2y}{dx^2} + \left(\frac{dy}{dx}\right)^2 = 0$       d)  $y \frac{d^2y}{dx^2} + \frac{dy}{dx} = 0$
20. If  $\frac{d^2y}{dx^2} \sin x = 0$ , then the solution of differential equation is  
 a)  $y = \sin x + cx + d$       b)  $y = \cos x + cx^2 + d$       c)  $y = \tan x + c$       d)  $y = \log \sin x + cx$